

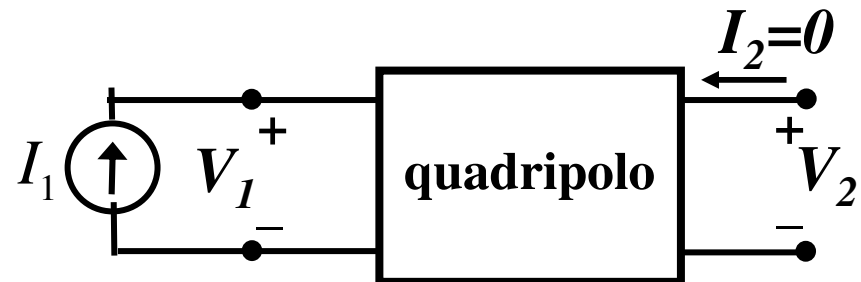
# QUADRIPOLOS



- **CARACTERIZAÇÃO:** Estabelecimento de relações que envolvam  $V_1$ ,  $I_1$ ,  $V_2$ ,  $I_2$ , no domínio da frequência, recorrendo-se à análise fasorial.
- **PARÂMETROS DE IMPEDÂNCIA ( $I_1, I_2$  variáveis independentes):**

$$\begin{cases} V_1 = Z_{11}I_1 + Z_{12}I_2 \\ V_2 = Z_{21}I_1 + Z_{22}I_2 \end{cases} \iff \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

$$Z_{11} = \left. \frac{V_1}{I_1} \right|_{I_2=0} \quad Z_{21} = \left. \frac{V_2}{I_1} \right|_{I_2=0}$$



# QUADRIPOLOS

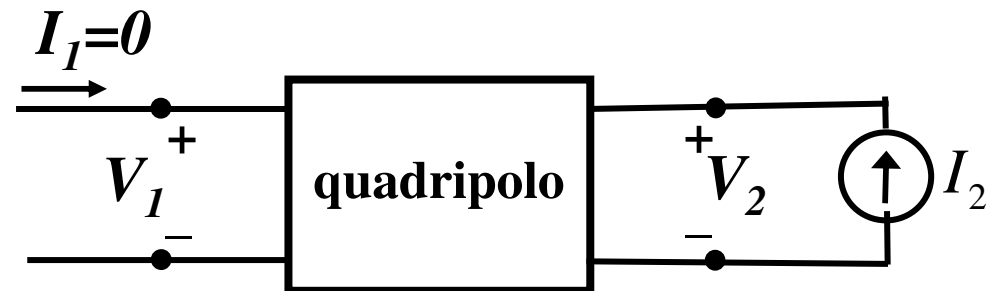


- PARÂMETROS DE IMPEDÂNCIA ( $I_1, I_2$  variáveis independentes):**

$$\begin{cases} V_1 = Z_{11}I_1 + Z_{12}I_2 \\ V_2 = Z_{21}I_1 + Z_{22}I_2 \end{cases} \iff \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

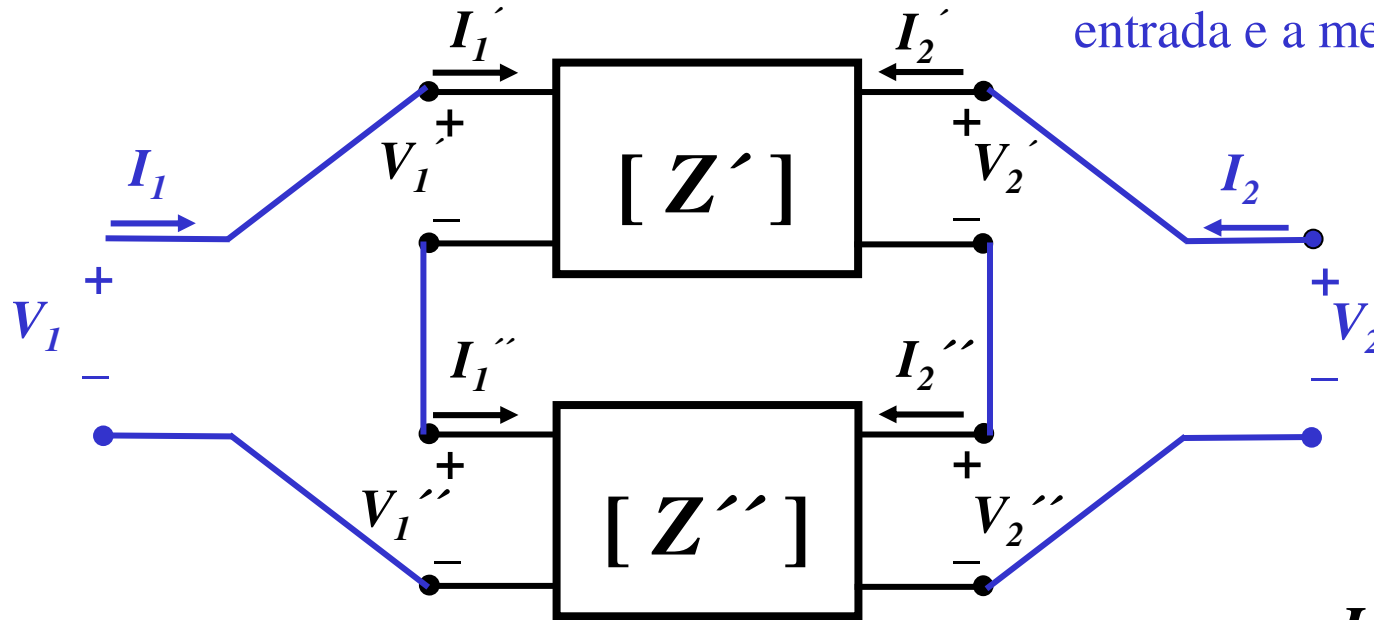
$$Z_{12} = \left. \frac{V_1}{I_2} \right|_{I_1=0}$$

$$Z_{22} = \left. \frac{V_2}{I_2} \right|_{I_1=0}$$

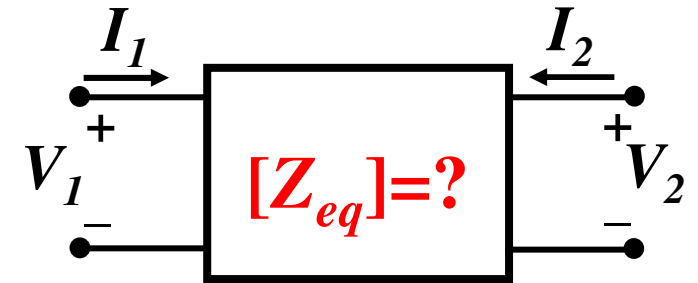


# QUADRIPOLOS

**LIGAÇÃO DE QUADRIPOLOS EM SÉRIE:** Partilham a mesma corrente de entrada e a mesma corrente de saída.



$$\begin{cases} V_1 = Z_{eq11} I_1 + Z_{eq12} I_2 \\ V_2 = Z_{eq21} I_1 + Z_{eq22} I_2 \end{cases}$$



$$[Z_{eq}] = [Z'] + [Z'']$$

$$Z_{eq11} = \left. \frac{V_1}{I_1} \right|_{I_2=0}$$

$$Z_{eq11} = Z'_{11} + Z''_{11}$$

$$Z_{eq22} = \left. \frac{V_2}{I_2} \right|_{I_1=0}$$

$$Z_{eq22} = Z'_{22} + Z''_{22}$$

$$Z_{eq21} = \left. \frac{V_2}{I_1} \right|_{I_2=0}$$

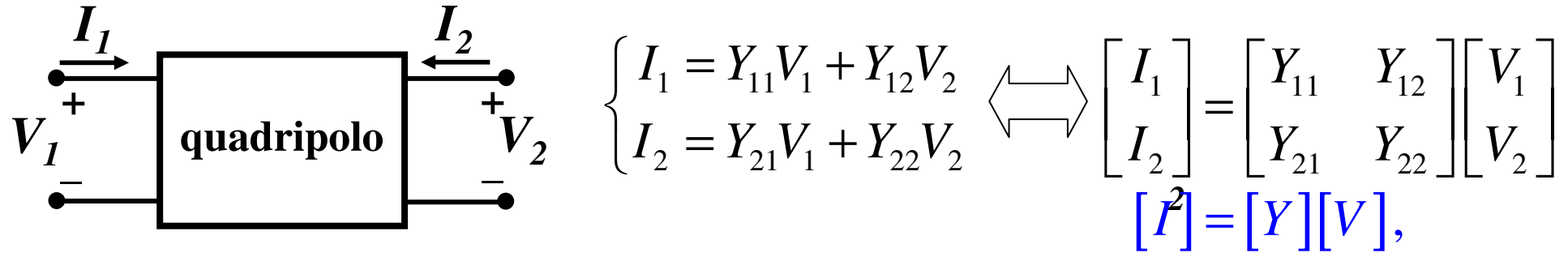
$$Z_{eq21} = Z'_{21} + Z''_{21}$$

$$Z_{eq12} = \left. \frac{V_1}{I_2} \right|_{I_1=0}$$

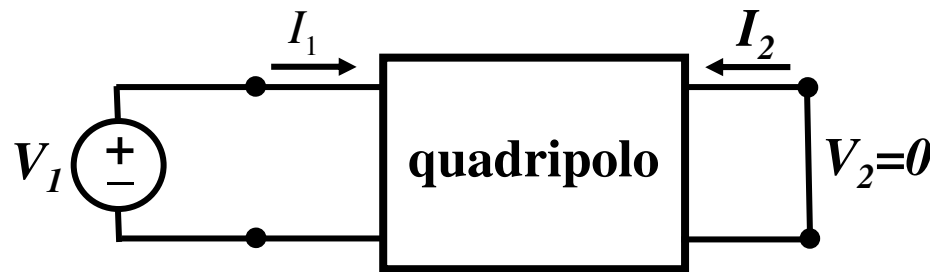
$$Z_{eq12} = Z'_{12} + Z''_{12}$$

# QUADRIPOLOS

## PARÂMETROS DE ADMITÂNCIA



**Y – Matriz de admitâncias**



$$Y_{11} = \left. \frac{I_1}{V_1} \right|_{V_2=0} \quad : \text{ Admitância de entrada}$$

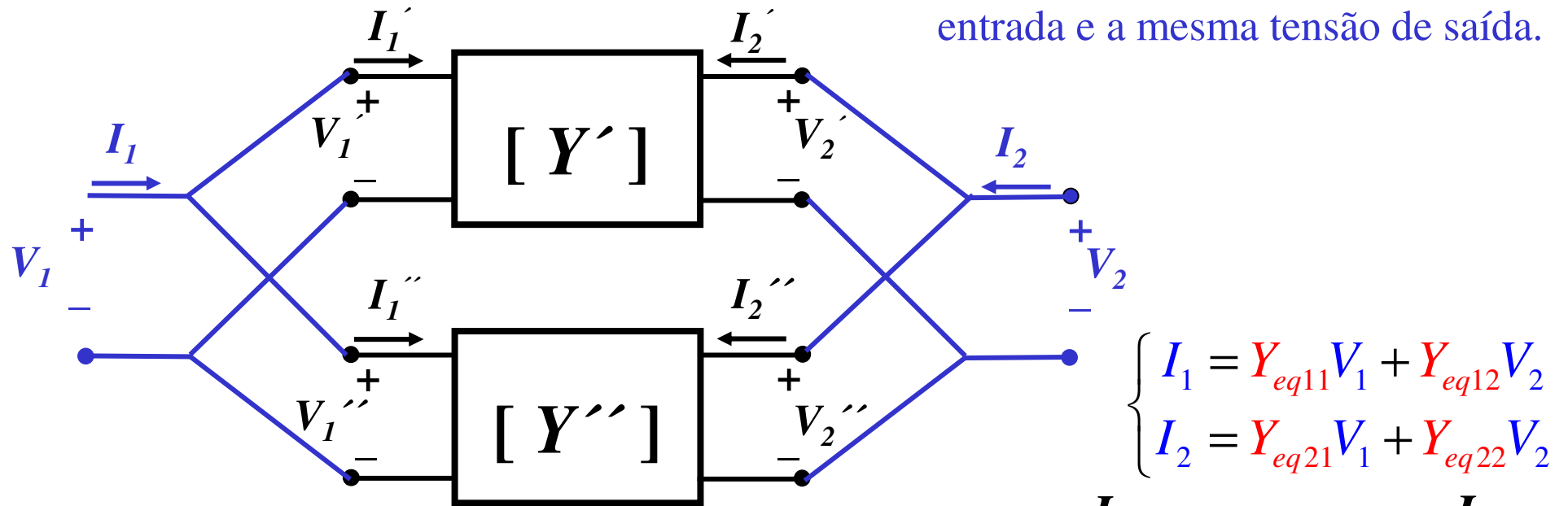
$$Y_{12} = \left. \frac{I_1}{V_2} \right|_{V_1=0} \quad : \text{ Admitância de transferência inversa}$$

$$Y_{21} = \left. \frac{I_2}{V_1} \right|_{V_2=0} \quad : \text{ Admitância de transferência directa}$$

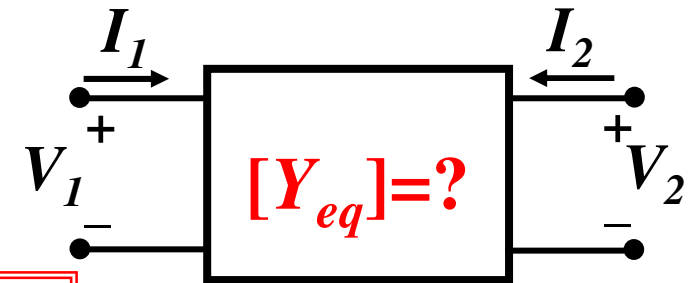
$$Y_{22} = \left. \frac{I_2}{V_2} \right|_{V_1=0} \quad : \text{ Admitância de saída}$$

# QUADRIPOLOS

**LIGAÇÃO DE QUADRIPOLOS EM PARALELO:** Partilham a mesma tensão de entrada e a mesma tensão de saída.



$$\begin{cases} I_1 = Y_{eq11} V_1 + Y_{eq12} V_2 \\ I_2 = Y_{eq21} V_1 + Y_{eq22} V_2 \end{cases}$$



$$Y_{eq11} = \left. \frac{I_1}{V_1} \right|_{V_2=0}$$

$$Y_{eq11} = Y'_{11} + Y''_{11}$$

$$Y_{eq22} = \left. \frac{I_2}{V_2} \right|_{V_1=0}$$

$$Y_{eq22} = Y'_{22} + Y''_{22}$$

$$\boxed{[Y_{eq}] = [Y'] + [Y'']}$$

$$Y_{eq21} = \left. \frac{I_2}{V_1} \right|_{V_2=0}$$

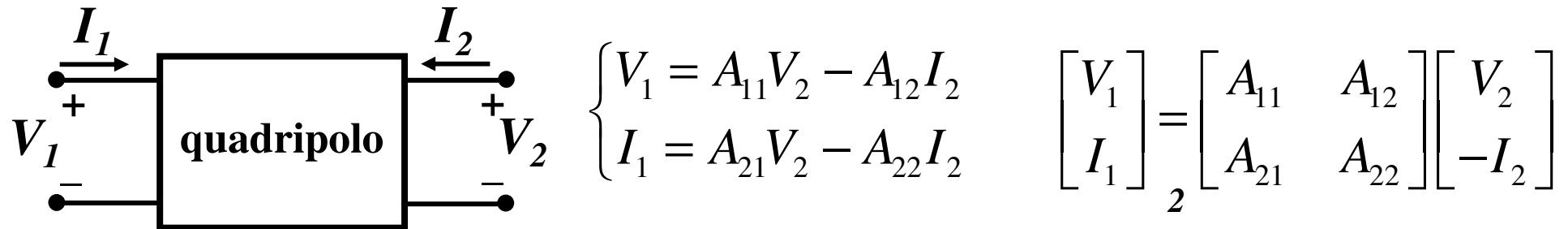
$$Y_{eq21} = Y'_{21} + Y''_{21}$$

$$Y_{eq12} = \left. \frac{I_1}{V_2} \right|_{V_1=0}$$

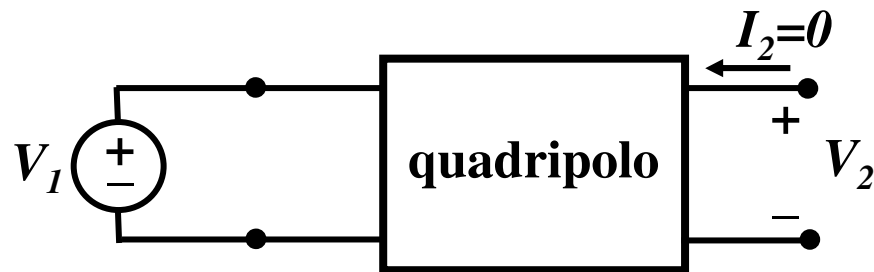
$$Y_{eq12} = Y'_{12} + Y''_{12}$$

# QUADRIPOLOS

## PARÂMETROS SÉRIE OU CASCATA

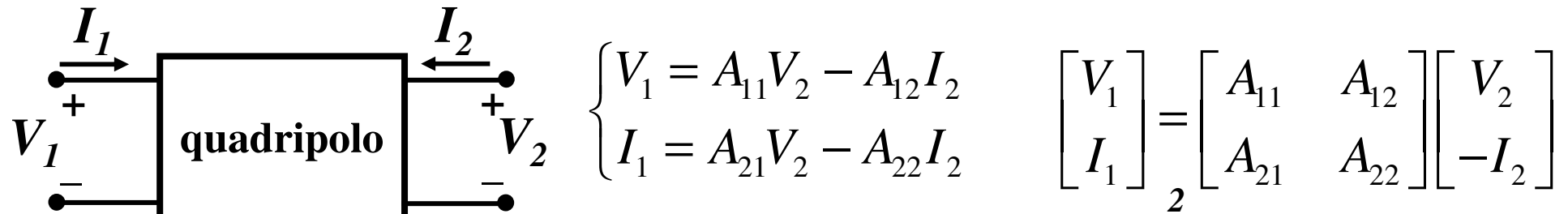


**A** – Matriz dos parâmetros série

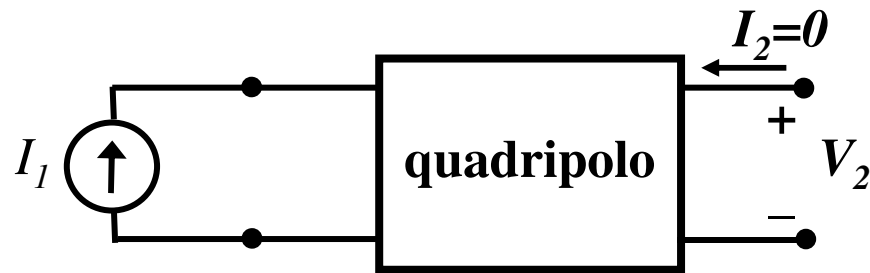


# QUADRIPOLOS

## PARÂMETROS SÉRIE OU CASCATA



**A** – Matriz dos parâmetros série



**Inverso do ganho de transimpedância.**



**Ganho de corrente inverso.**