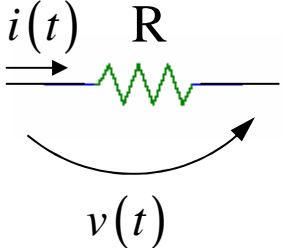
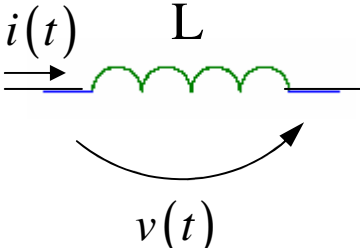
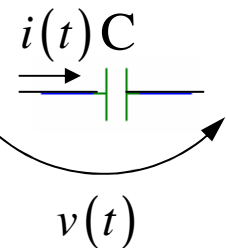
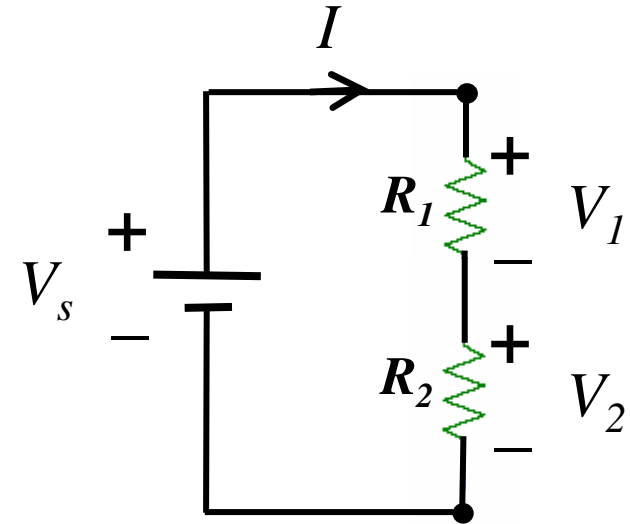


# ANÁLISE DE CIRCUITOS

## ASSOCIAÇÃO DE ELEMENTOS PASSIVOS

Resistência	Bobina	Condensador
		
$v(t) = Ri(t)$	$v(t) = L \frac{di(t)}{dt}$	$i(t) = C \frac{dv(t)}{dt}$

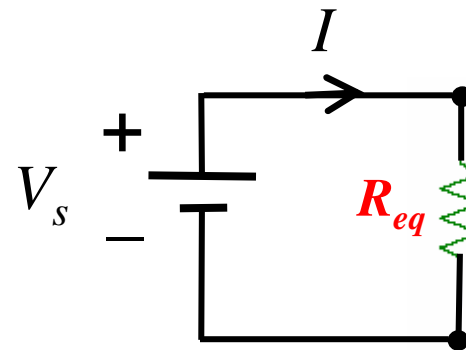


- RESISTÊNCIAS EM SÉRIE:**

$$-V_s + R_1 I + R_2 I = 0$$

$$V_s = \underbrace{(R_1 + R_2)}_{R_{eq}} I$$

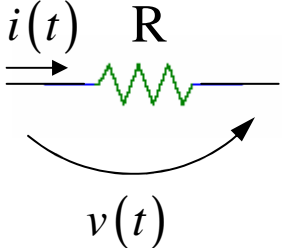
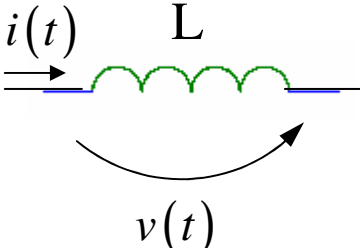
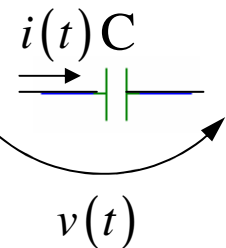
$$V_s = R_{eq} I$$

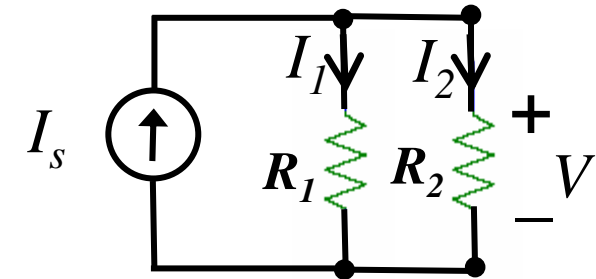


$$R_{eq} = \sum_{k=1}^N R_k$$

# ANÁLISE DE CIRCUITOS

## ASSOCIAÇÃO DE ELEMENTOS PASSIVOS

Resistência	Bobina	Condensador
		
$v(t) = Ri(t)$	$v(t) = L \frac{di(t)}{dt}$	$i(t) = C \frac{dv(t)}{dt}$



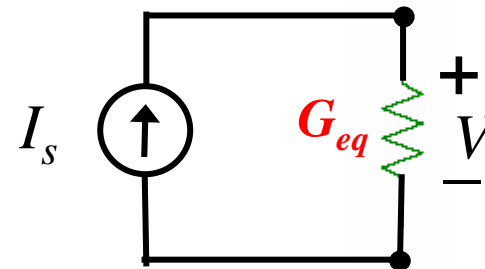
- RESISTÊNCIAS EM PARALELO  $\left( I = GV, \quad G = \frac{1}{R} \right)$ :

$$-I_s + I_1 + I_2 = 0$$

$$I_s = G_1 V + G_2 V$$

$$I_s = \underbrace{(G_1 + G_2)}_{G_{eq}} V$$

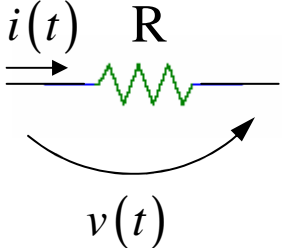
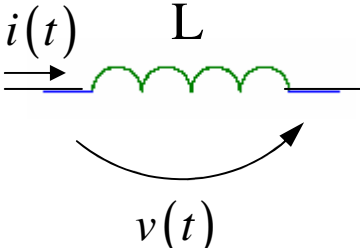
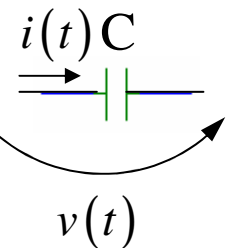
$$I_s = G_{eq} V$$

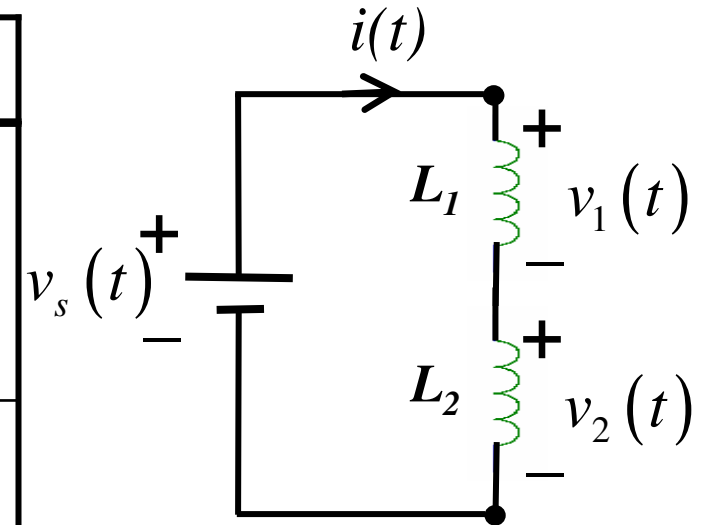


$$G_{eq} = \sum_{k=1}^N G_k$$

# ANÁLISE DE CIRCUITOS

## ASSOCIAÇÃO DE ELEMENTOS PASSIVOS

Resistência	Bobina	Condensador
		
$v(t) = Ri(t)$	$v(t) = L \frac{di(t)}{dt}$	$i(t) = C \frac{dv(t)}{dt}$



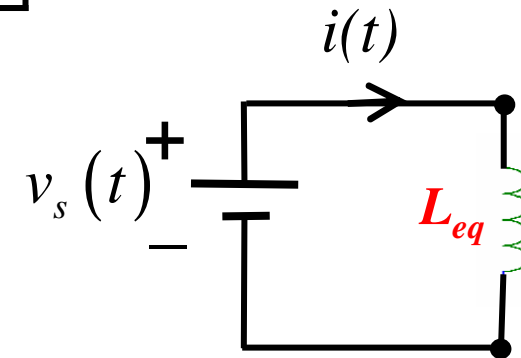
### • BOBINAS EM SÉRIE:

$$-v_s(t) + v_1(t) + v_2(t) = 0$$

$$v_s(t) = L_1 \frac{di(t)}{dt} + L_2 \frac{di(t)}{dt}$$

$$v_s(t) = \underbrace{(L_1 + L_2)}_{L_{eq}} \frac{di(t)}{dt}$$

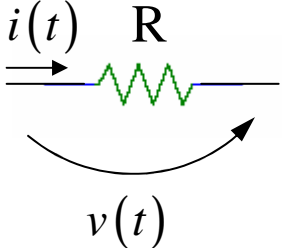
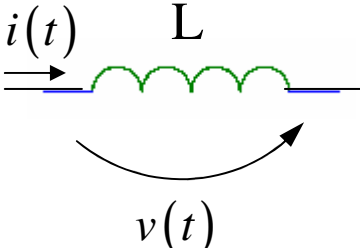
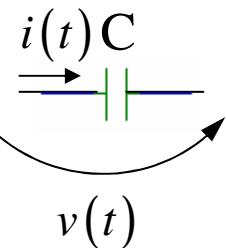
$$v_s(t) = L_{eq} \frac{di(t)}{dt}$$

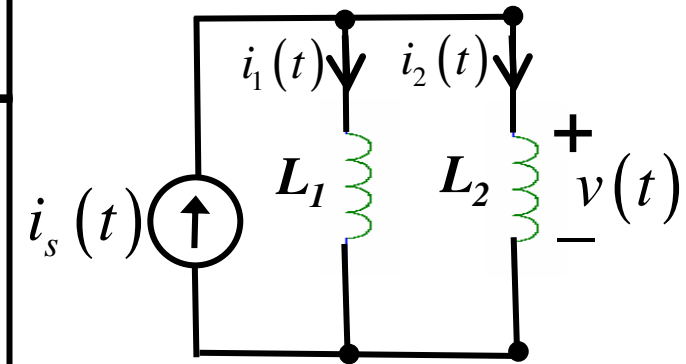


$$L_{eq} = \sum_{k=1}^N L_k$$

# ANÁLISE DE CIRCUITOS

## ASSOCIAÇÃO DE ELEMENTOS PASSIVOS

Resistência	Bobina	Condensador
		
$v(t) = Ri(t)$	$v(t) = L \frac{di(t)}{dt}$	$i(t) = C \frac{dv(t)}{dt}$



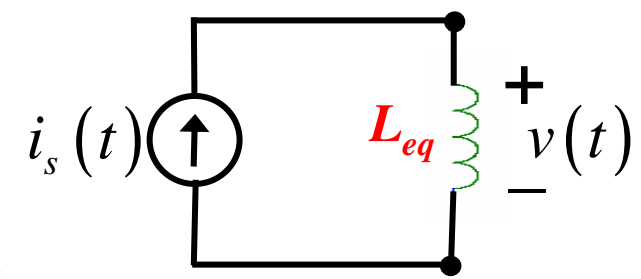
• **BOBINAS EM PARALELO**  $\left( i(t) = \frac{1}{L} \int_0^t v(t) dt \right)$ :

$$i_s(t) - i_1(t) - i_2(t) = 0$$

$$i_s(t) = \left( \frac{1}{L_1} + \frac{1}{L_2} \right) \int_0^t v(t) dt$$

$$\underbrace{\hspace{10em}}_{1/L_{eq}}$$

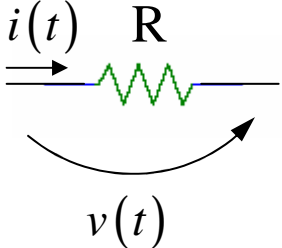
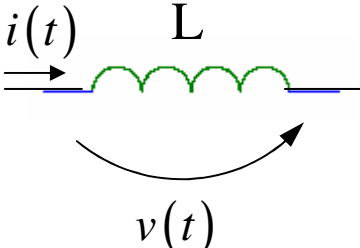
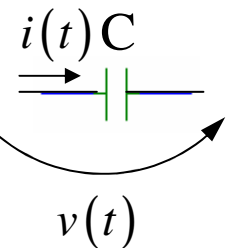
$$i_s(t) = \frac{1}{L_{eq}} \int_0^t v(t) dt$$

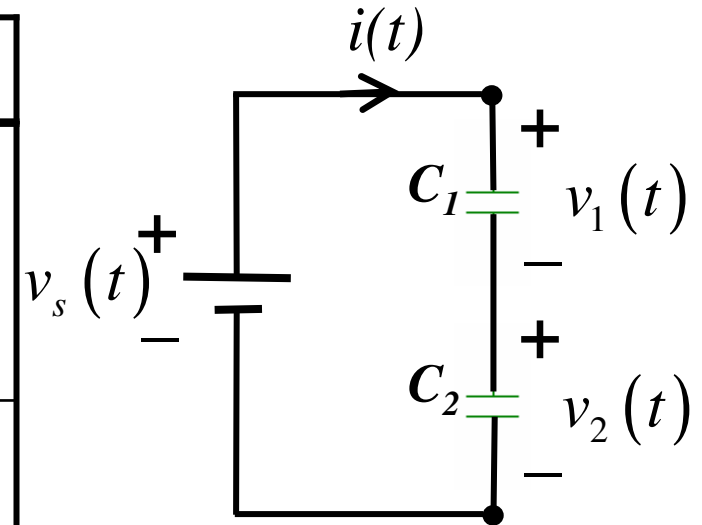


$$\frac{1}{L_{eq}} = \sum_{k=1}^N \frac{1}{L_k}$$

# ANÁLISE DE CIRCUITOS

## ASSOCIAÇÃO DE ELEMENTOS PASSIVOS

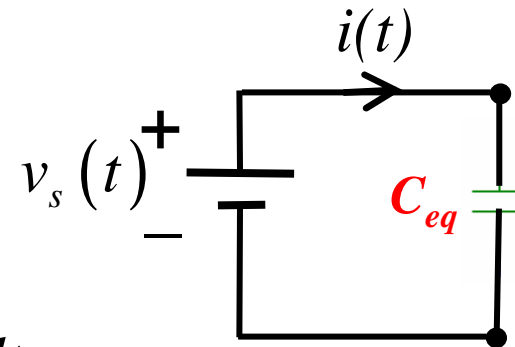
Resistência	Bobina	Condensador
		
$v(t) = Ri(t)$	$v(t) = L \frac{di(t)}{dt}$	$i(t) = C \frac{dv(t)}{dt}$



- CONDENSADORES EM SÉRIE  $\left( v(t) = \frac{1}{C} \int_0^t i(t) dt \right)$ :

$$-v_s(t) + v_1(t) + v_2(t) = 0$$

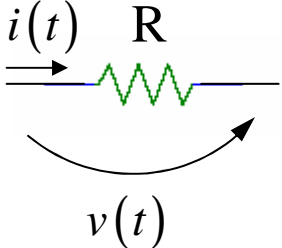
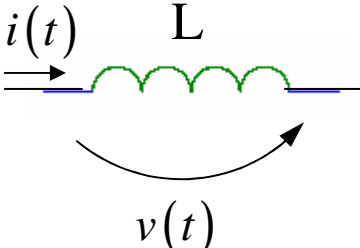
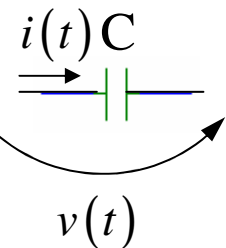
$$v_s(t) = \underbrace{\left( \frac{1}{C_1} + \frac{1}{C_2} \right)}_{1/C_{eq}} \int_0^t i(t) dt \quad v_s(t) = \frac{1}{C_{eq}} \int_0^t i(t) dt$$

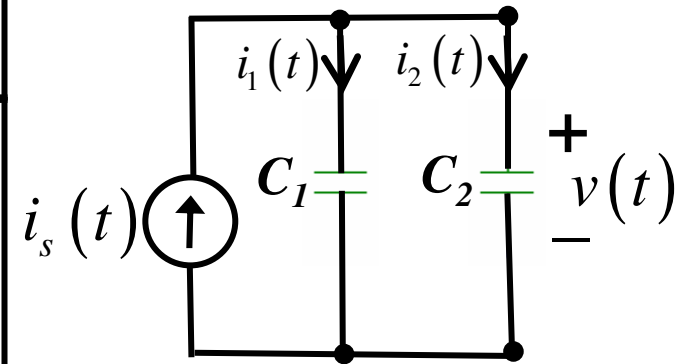


$$\frac{1}{C_{eq}} = \sum_{k=1}^N \frac{1}{C_k}$$

# ANÁLISE DE CIRCUITOS

## ASSOCIAÇÃO DE ELEMENTOS PASSIVOS

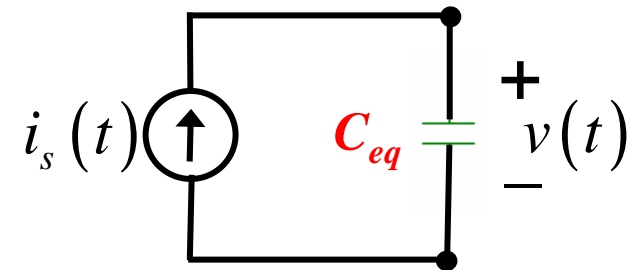
Resistência	Bobina	Condensador
		
$v(t) = Ri(t)$	$v(t) = L \frac{di(t)}{dt}$	$i(t) = C \frac{dv(t)}{dt}$



- CONDENSADORES EM PARALELO:**

$$i_s(t) - i_1(t) - i_2(t) = 0$$

$$i_s(t) = \underbrace{(C_1 + C_2)}_{C_{eq}} \frac{dv(t)}{dt} \quad i_s(t) = C_{eq} \frac{dv(t)}{dt}$$

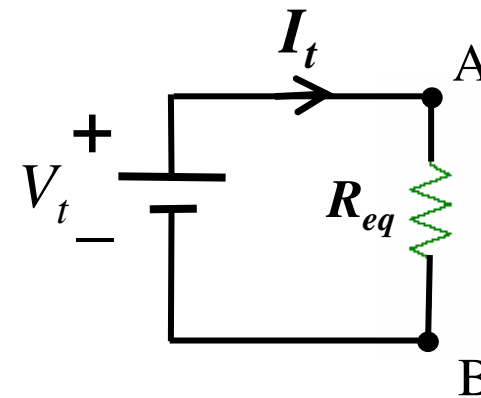
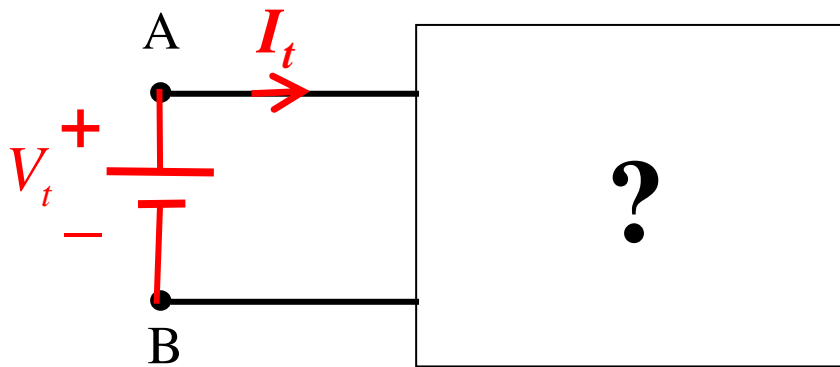


$$C_{eq} = \sum_{k=1}^N C_k$$

# ANÁLISE DE CIRCUITOS

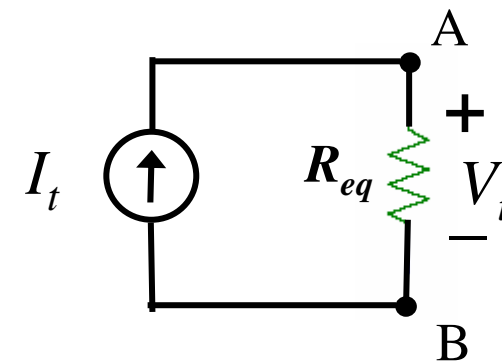
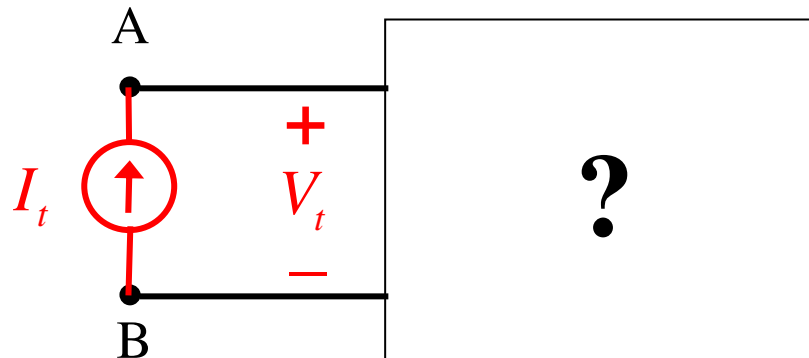
## ASSOCIAÇÃO DE ELEMENTOS PASSIVOS

### CIRCUITO RESISTIVO DE COMPLEXIDADE ARBITRÁRIA



$$R_{eq} = \frac{V_t}{I_t}$$

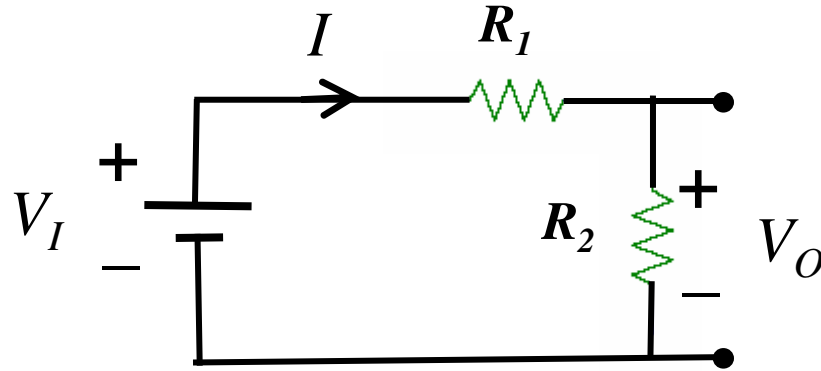
ou, alternativamente:



# ANÁLISE DE CIRCUITOS

## DIVISOR DE TENSÃO

Qual a tensão de saída  $V_o$  quando aos terminais da série se aplica  $V_I$  ?



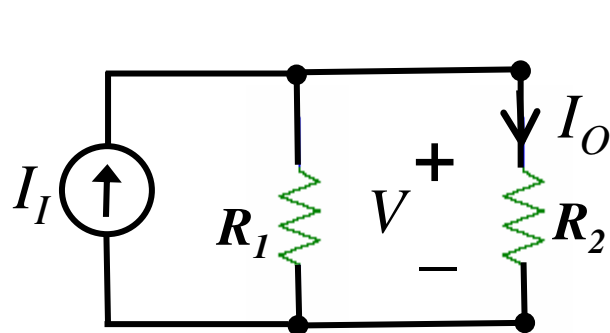
$$-V_I + R_1 I + R_2 I = 0$$

$$V_I = (R_1 + R_2) I \quad \text{mas: } I = \frac{V_o}{R_2}$$

$$V_o = \frac{R_2}{R_1 + R_2} V_I$$

## DIVISOR DE CORRENTE

Qual a corrente de saída  $I_o$  quando entra no nó a corrente  $I_I$  ?

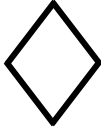


$$I_I = \frac{V}{R_1} + \frac{V}{R_2} = \left( \frac{1}{R_1} + \frac{1}{R_2} \right) V \quad \text{mas: } V = R_2 I_o$$

$$I_o = \frac{R_1}{R_1 + R_2} I_I$$

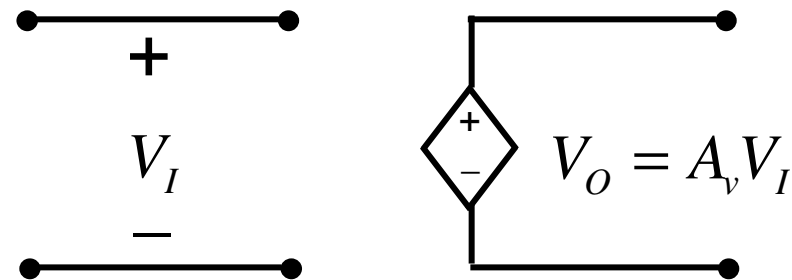


## ELEMENTOS DE CIRCUITO

- elementos activos {
- Fontes de tensão
  - Fontes de corrente
- ✓ Independentes  
 ✓ **Dependentes** 

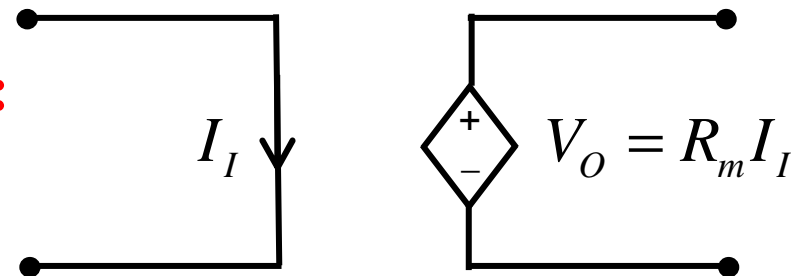
### Fontes de:

- **Tensão** controladas por **tensão**:



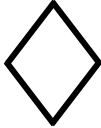
$A_v$  – ganho de tensão

- **Tensão** controladas por **corrente**:



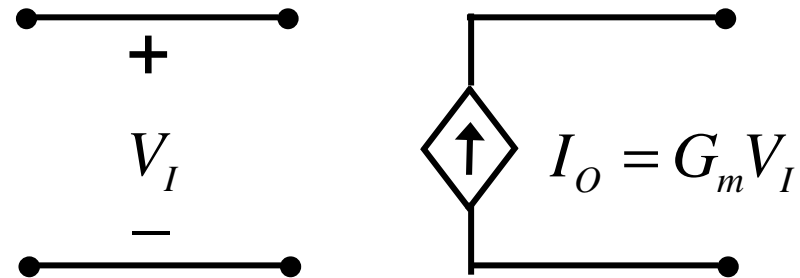
$R_m$  – ganho de trans-impedância

## ELEMENTOS DE CIRCUITO

- elementos activos {
- Fontes de tensão
  - Fontes de corrente
- ✓ Independentes
- ✓ Dependentes 

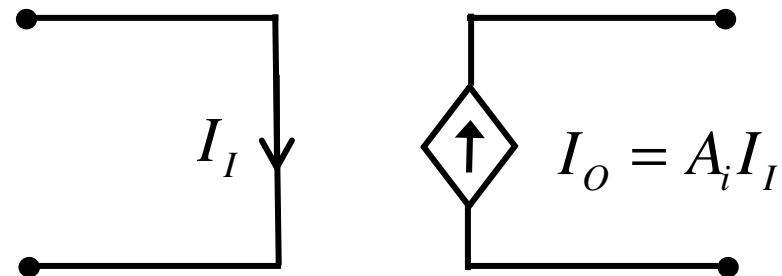
### Fontes de:

- **Corrente** controladas por **tensão**



$G_m$  – ganho de trans-condutância

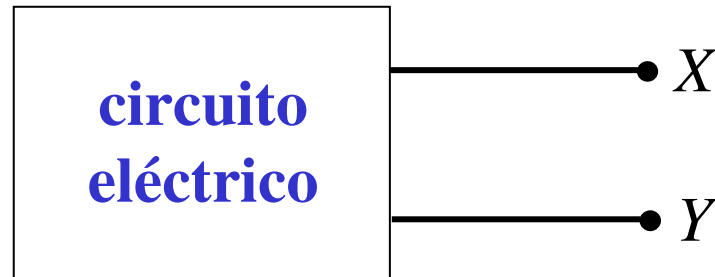
- **Corrente** controladas por **corrente**



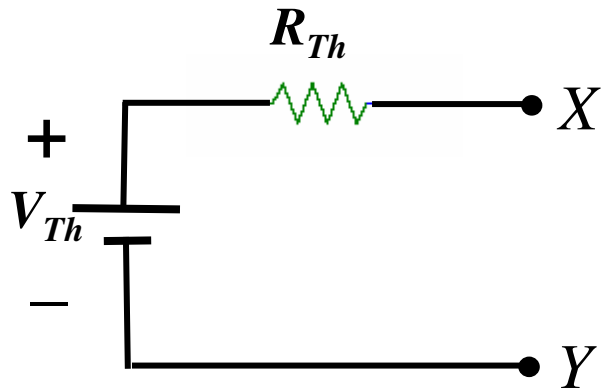
$A_i$  – ganho de corrente

## ANÁLISE DE CIRCUITOS

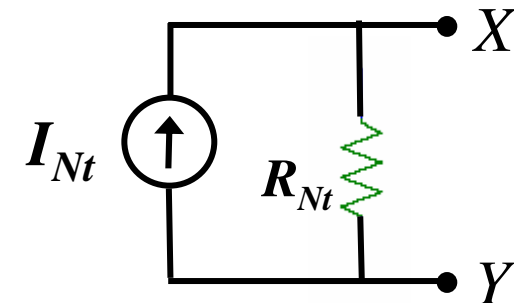
### circuito eléctrico formado por resistências e fontes independentes:



#### TEOREMA DE THÉVENIN:



#### TEOREMA DE NORTON:



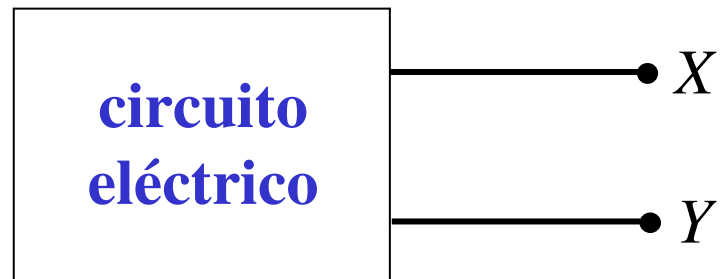
$$V_{Th} = R_{Th} I_{Nt}$$

- $V_{th}$  (tensão de Thévenin): tensão em circuito aberto aos terminais  $X$  e  $Y$ .
- $R_{Th} = R_{Nt}$  (resistência equivalente): vista a partir dos terminais  $X$  e  $Y$  com todas as fontes independentes anuladas.
- $I_{Nt}$  (corrente de Norton): corrente em curto-circuito entre os terminais  $X$  e  $Y$ .

## ANÁLISE DE CIRCUITOS

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circuito eléctrico formado por resistências e fontes independentes:



**TEOREMA DA SOBREPOSIÇÃO**